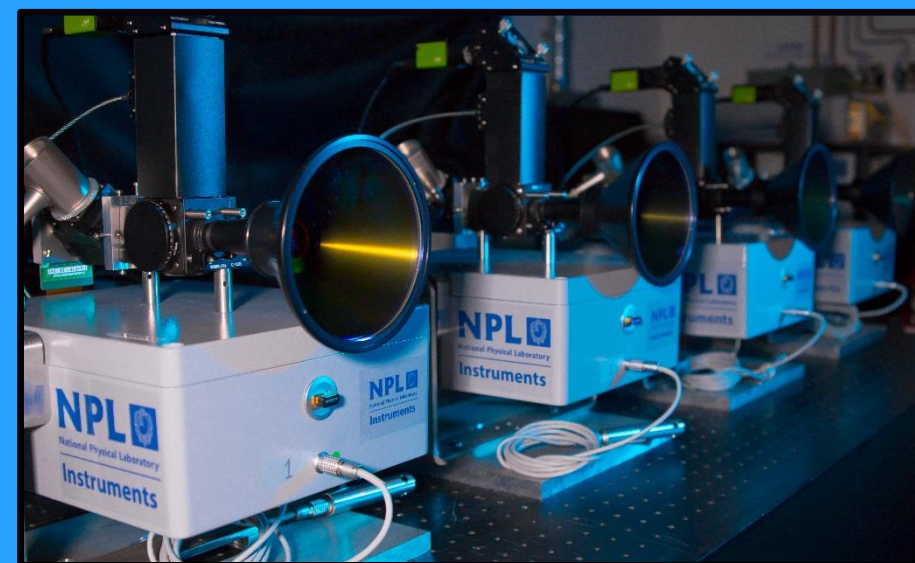


## Frequency Scanning Interferometry – traceable 3D coordinate metrology

Ben Hughes, Mike Campbell, Andrew Lewis

LUMINAR End of Project Meeting  
2016, 19<sup>th</sup> May, NPL



# Outline

- Introduction
- NPL's Proposed Coordinate Metrology System
- Results
- Summary & Conclusions
- Future Work

# Introduction

- How good is my instrument?
- How can I be sure my calibration is still valid?
- What's my measurement uncertainty?

# Introduction

- Objective is to make a CMS that is:
  1. As **accurate** as possible
  2. Measures **multiple points** simultaneously
  3. **Self-calibrating** - built-in compensation for systematic errors
  4. Has built-in **traceability** to SI metre
  5. Gives on-line **uncertainty estimation**
- Current project focus on proof-of-principle

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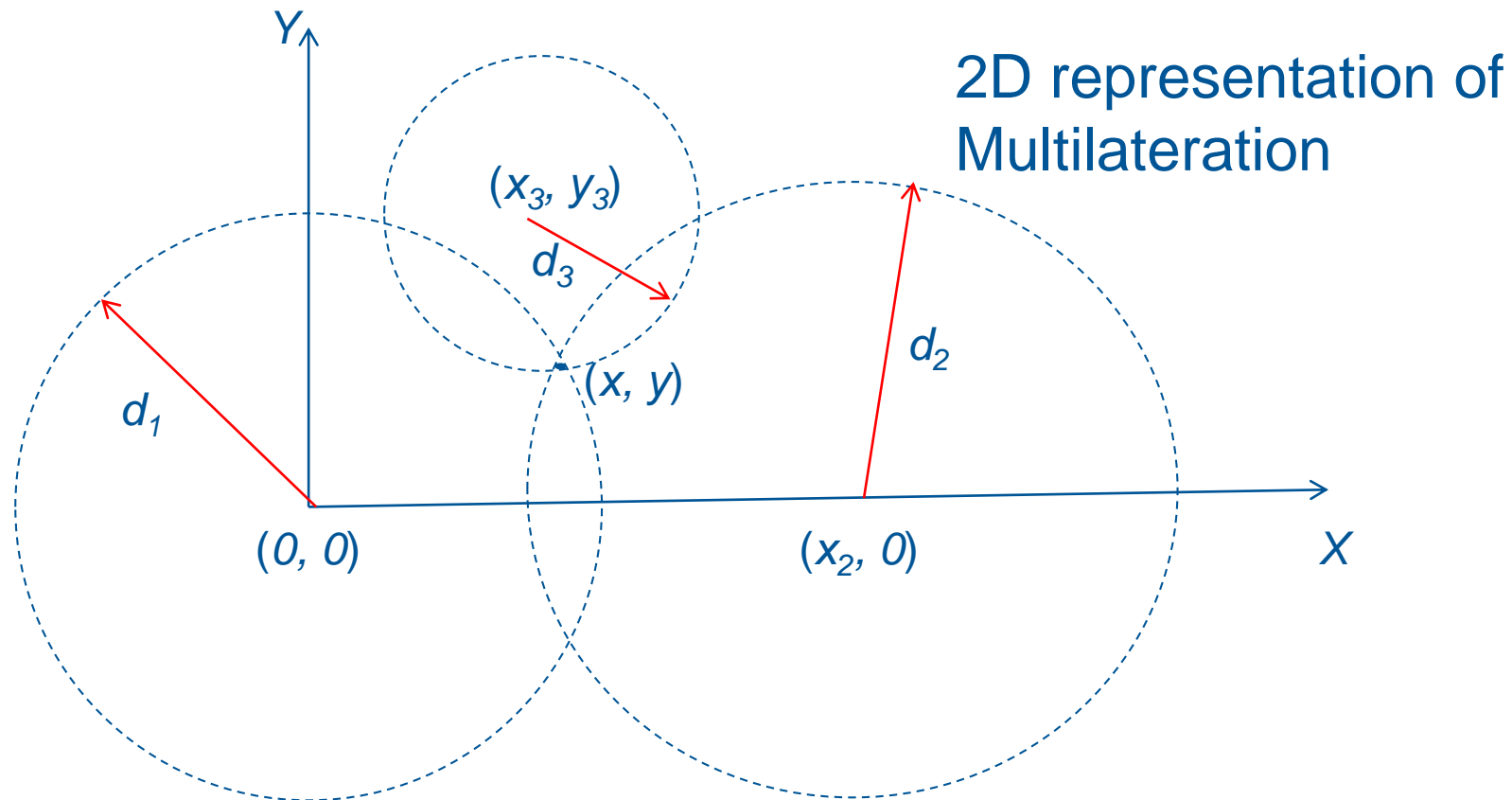
# Proposed solution

- Combination of:
  - Multilateration
    - calculates coordinates from distances
    - self calibrating
  - Frequency scanning interferometry
    - high accuracy range measurement



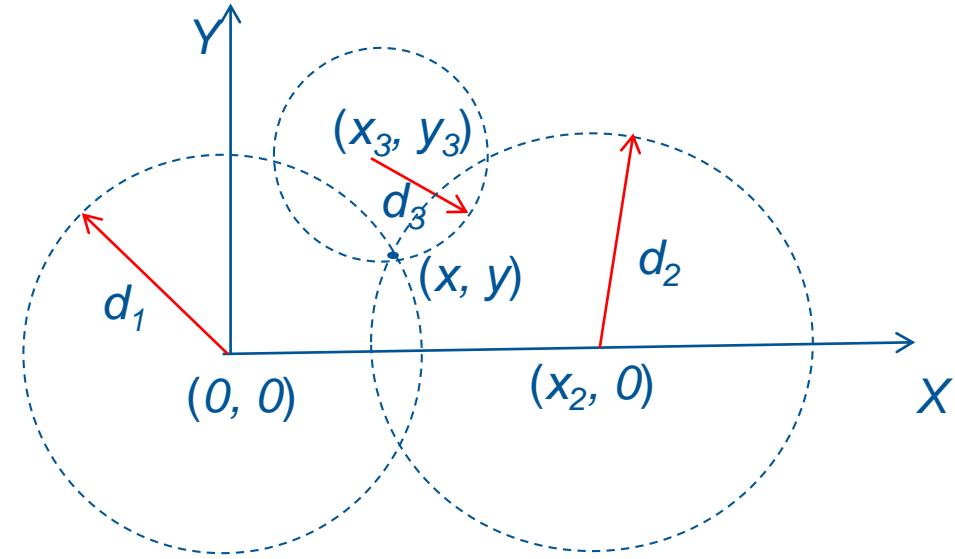
# Multilateration...

- ... is the process of determining absolute (or relative) locations of points by measurement of **distances** using the geometry of circles or spheres



# Multilateration

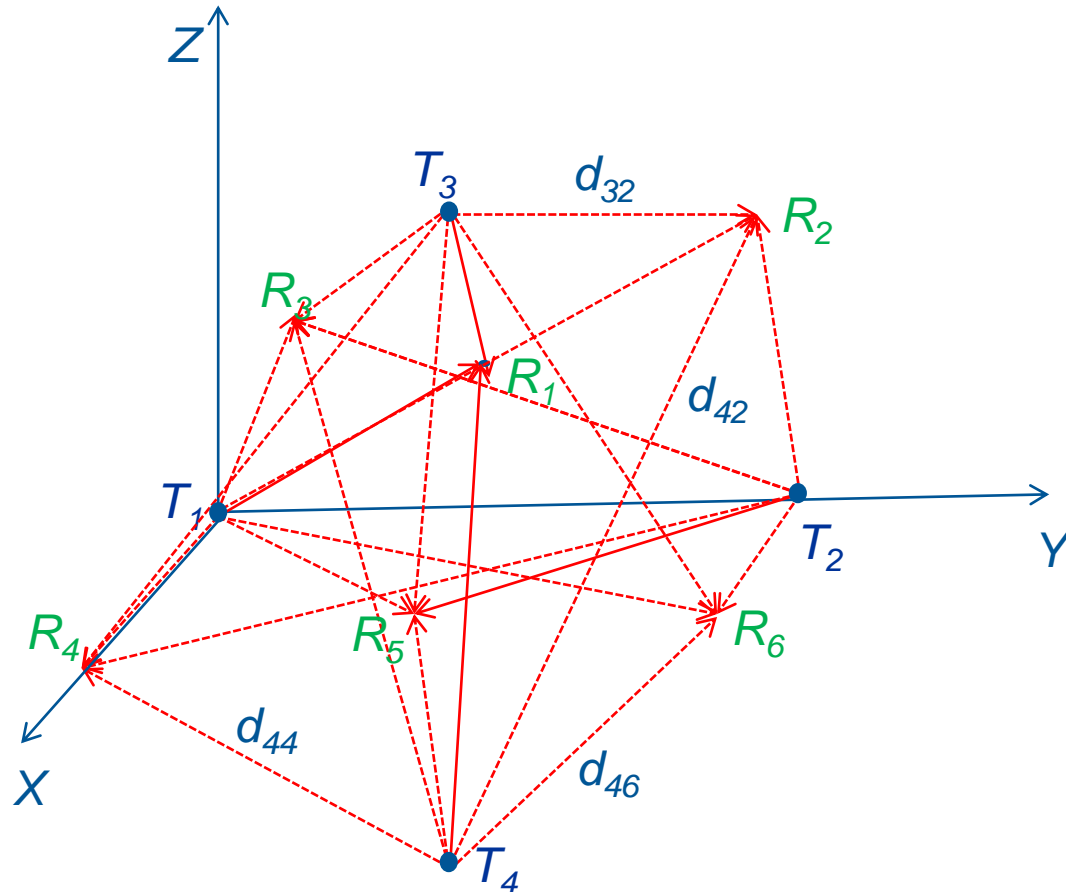
- *If instrument locations are known e.g.*
  - Origin
  - Distance  $x_2$  along x axis
  - On X-Y plane at  $(x_3, y_3)$
- Then measurements  $d_1$ ,  $d_2$  and  $d_3$  are sufficient to locate uniquely target coordinates  $(x, y)$
- In 3D and if instrument locations are **not known**, we need more information...





# Multilateration

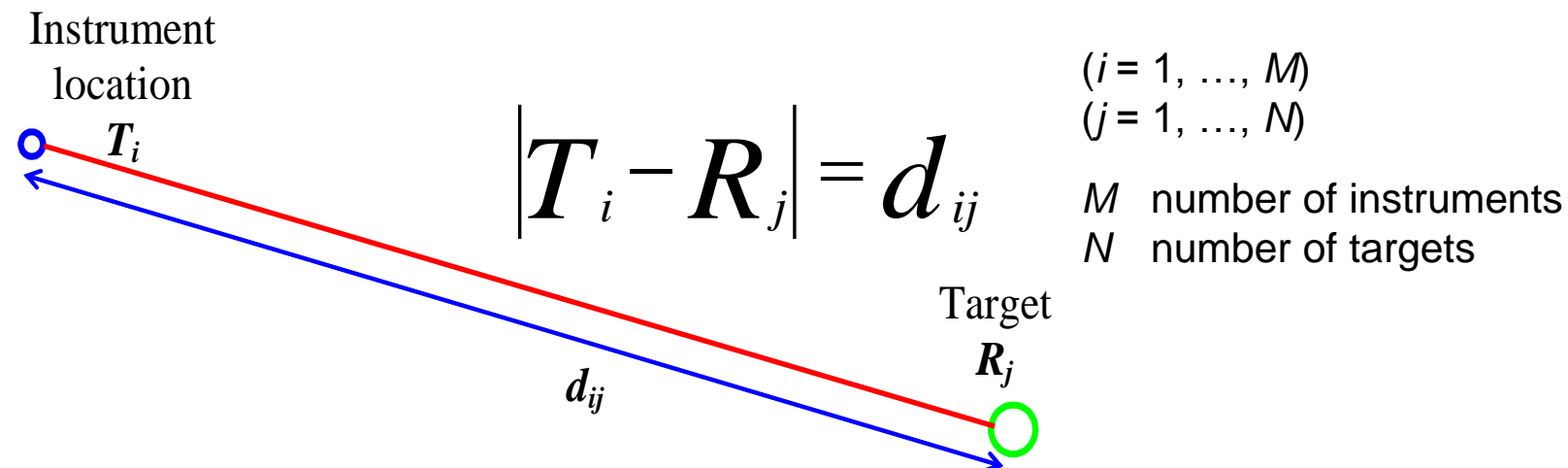
- Add a **fourth** instrument at a fourth location, and
- Measure ranges to **multiple** targets



$R_j$  –  $j^{\text{th}}$  target coordinates  
 $T_i$  –  $i^{\text{th}}$  Instrument coordinates  
 $d_{ij}$  – measured distance from  
 $i^{\text{th}}$  instrument to  $j^{\text{th}}$  target

# Multilateration

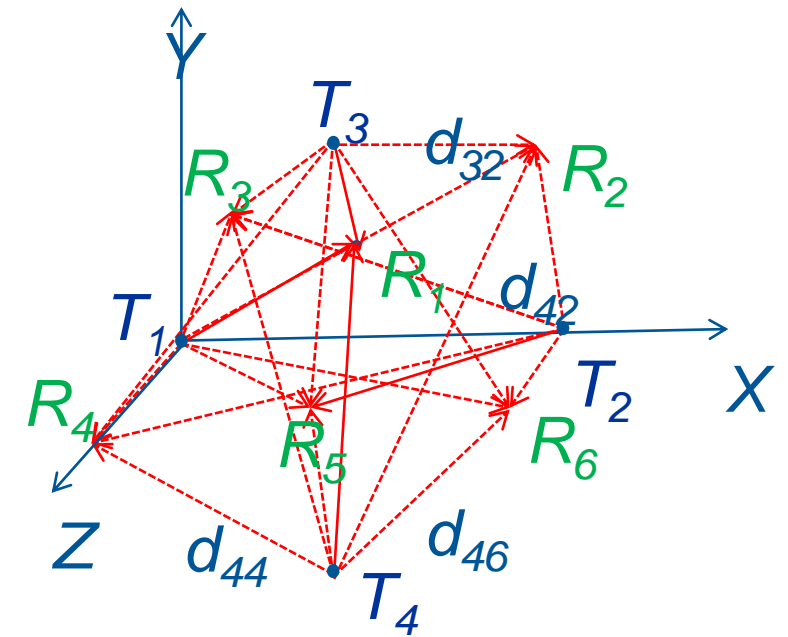
- Determine coordinates by measuring range,  $d_{ij}$  from  $M$  instrument locations,  $T_i$ , to  $N$  targets located at coordinates  $R_j$ .
  - **Self-calibrating** if  $M \geq 4$  and  $N \geq 6$
  - Increasing  $N$ ,  $M$  gives data redundancy -> **uncertainty estimates**
  - **Traceable to SI** (if  $d_{ij}$  is traceable)
  - Can extend model equation to include other **systematic factors** – and **compensate** for them with full **traceability**
  - Coordinate uncertainty  $\approx$  range uncertainty



# Multilateration

Determine coordinates by measuring range,  $d_{ij}$  from  $M$  instrument locations,  $T_i$ , to  $N$  targets located at coordinates  $R_j$ .

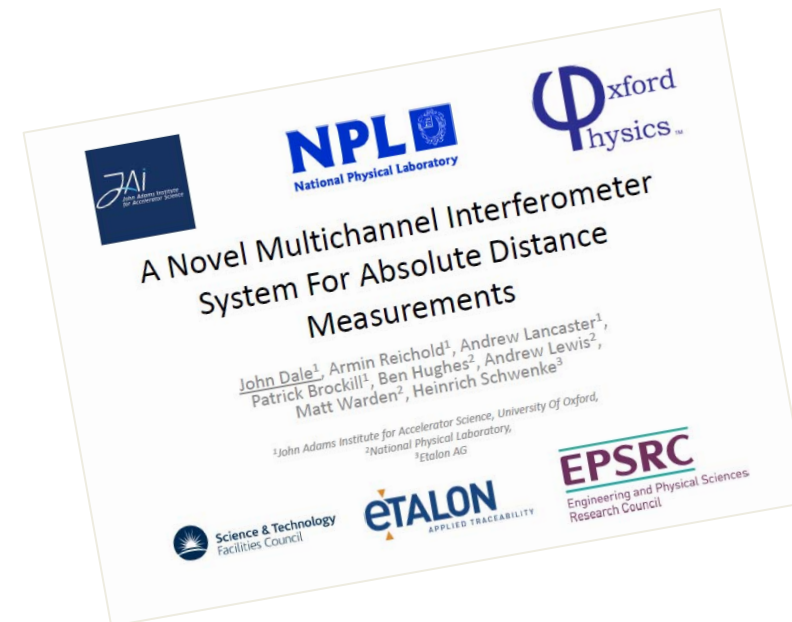
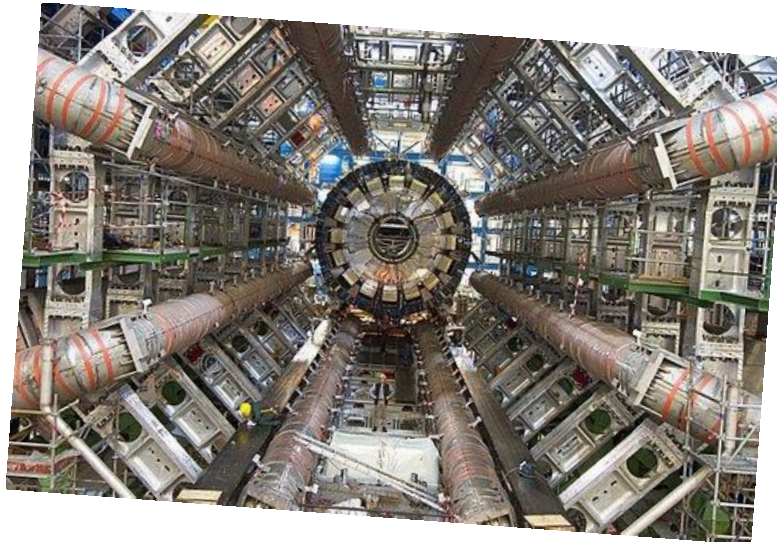
- **Self-calibrating** if  $M \geq 4$  and  $N \geq 6$
- Increasing  $N, M$  gives data redundancy -> **uncertainty estimates**
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- Can extend model equation to include other **systematic factors** – and **compensate** for them with full **traceability**
- Can achieve coordinate uncertainty  $\approx$  range uncertainty



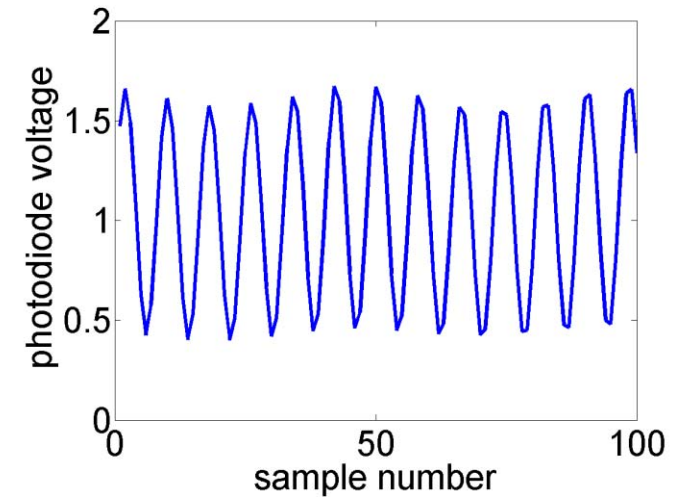
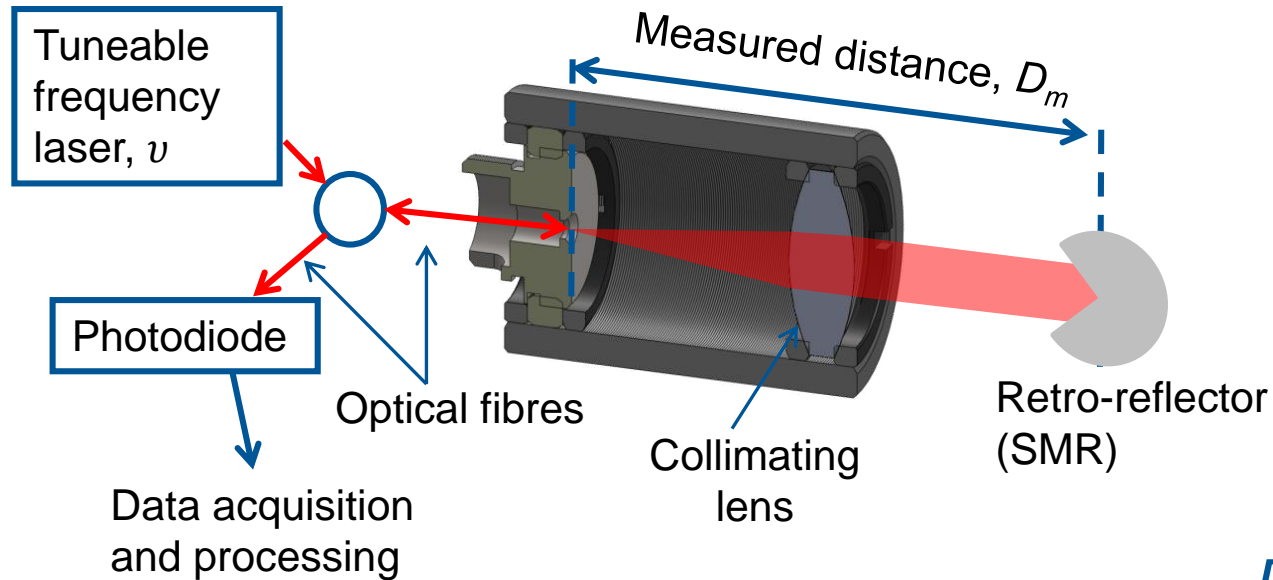
**How do we determine absolute distance to multiple targets simultaneously?**

# Frequency Scanning Interferometry

- Developed extensively at Oxford University
  - ATLAS
  - Oxford/NPL/Etalon presented recent developments at LVMC 2012
- Similar to laser radar technology



# Conventional Frequency Scanning Interferometry (FSI)



$$D = c \frac{N}{2\Delta\nu}$$

$D$  = measured distance

$c$  = speed of light (defined)

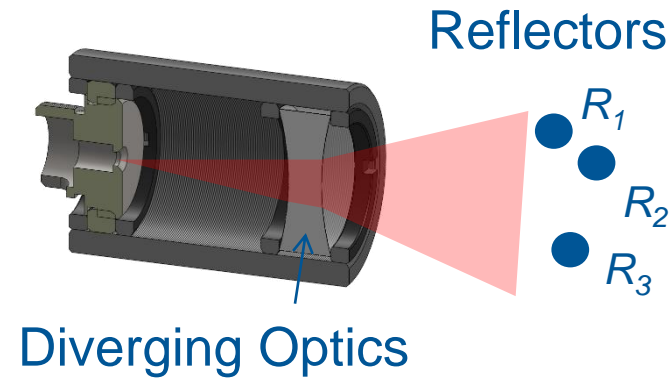
$N$  = Number of cycles of signal

$\Delta\nu$  = change in laser frequency

# Measuring multiple targets simultaneously

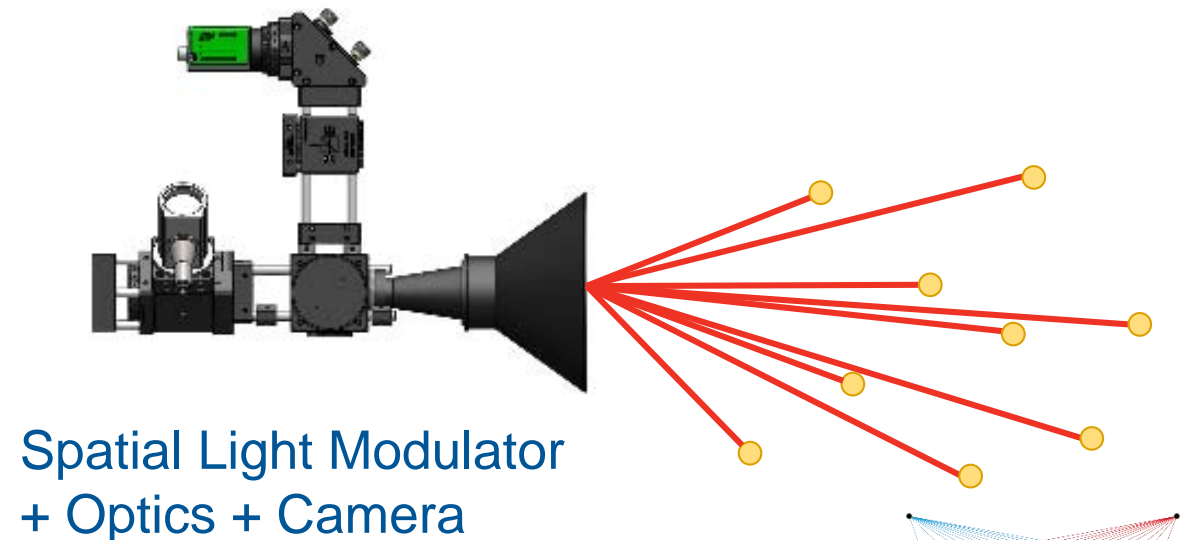
## Short range

- Divergent lens system
- Cheap sensor heads



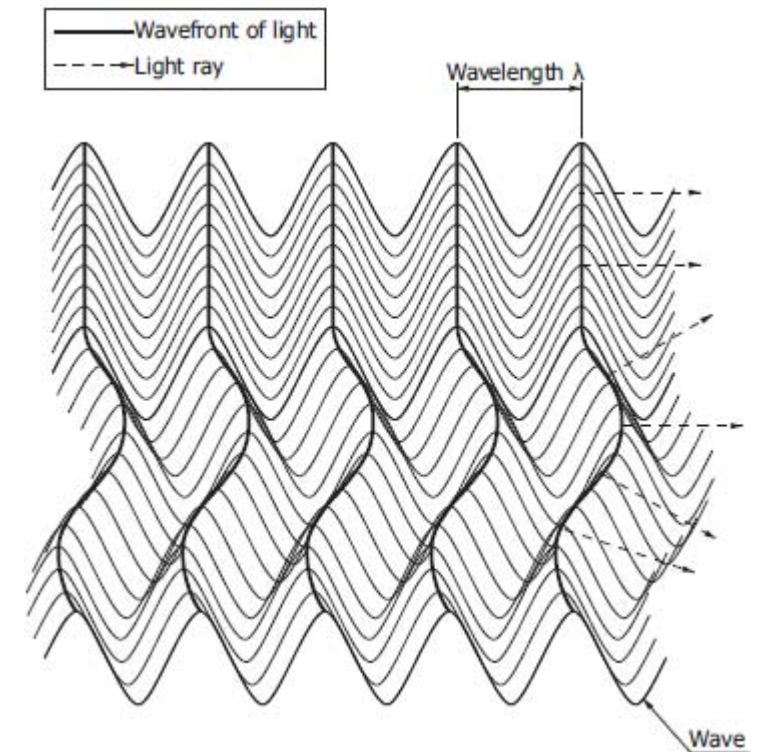
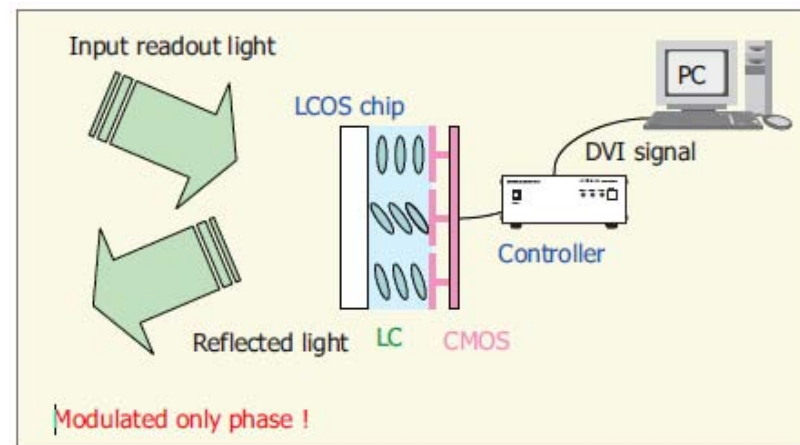
## Long range

- Near-collimated beams
- Multiple beams
- Steerable beams with tracking

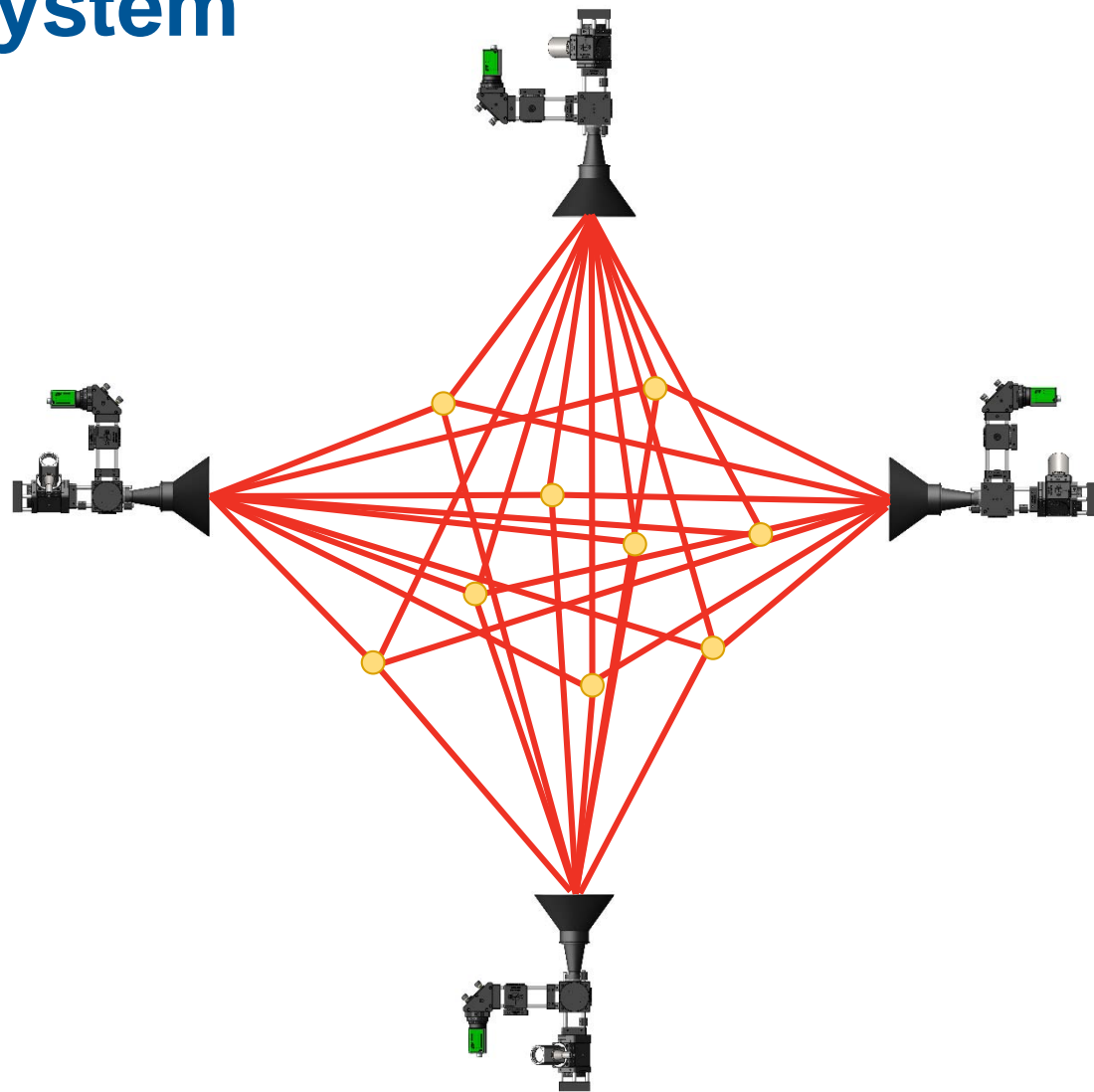


# Measuring multiple targets simultaneously

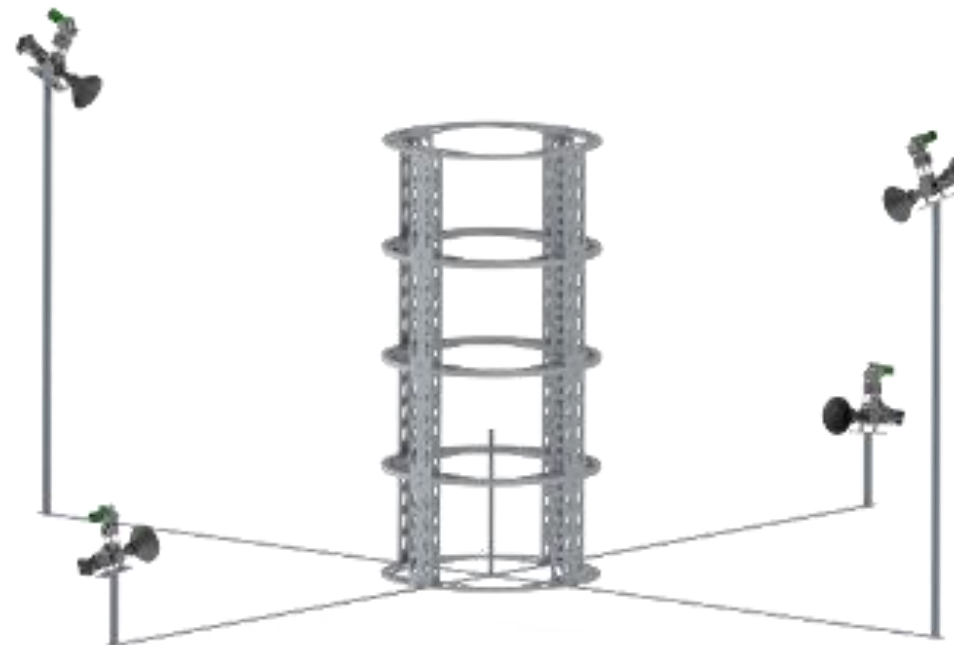
- Key component is the SLM



# NPL's Proposed Coordinate Metrology System

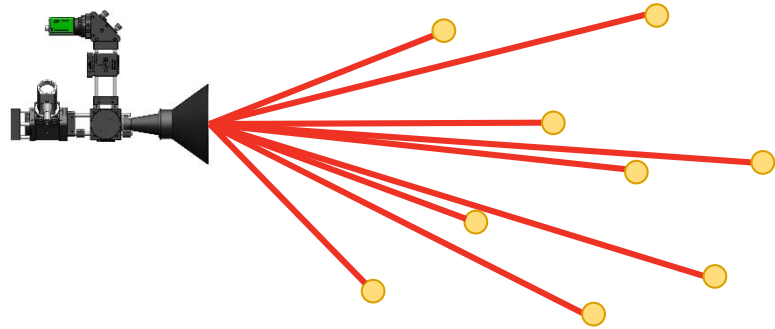


Aim for an operating volume of 10 m x 10 m x 5 m and uncertainty of  $< 50 \mu\text{m}$

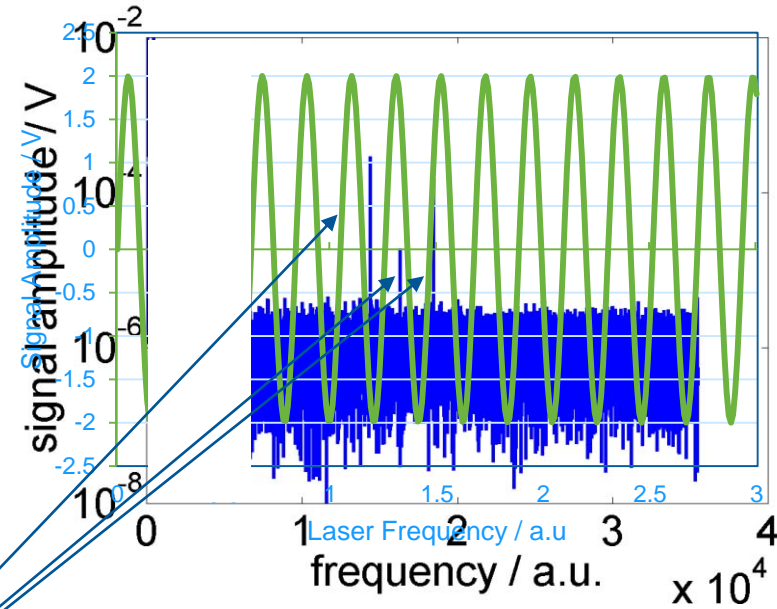




# Extracting signals from multiple targets



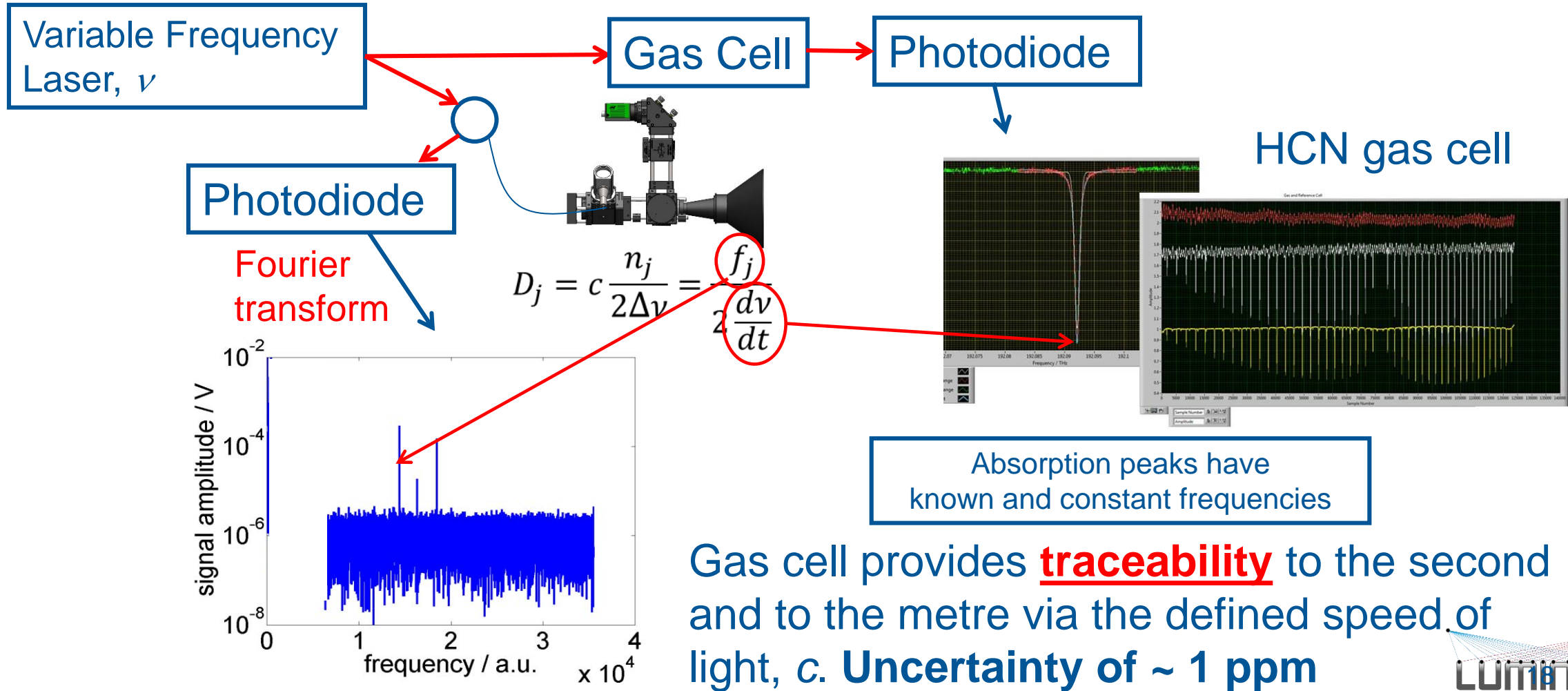
Each target shows up as a separate peak in the frequency domain



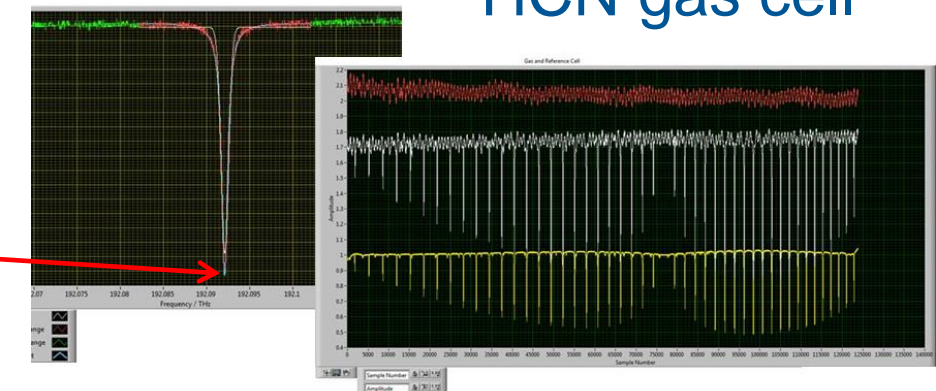
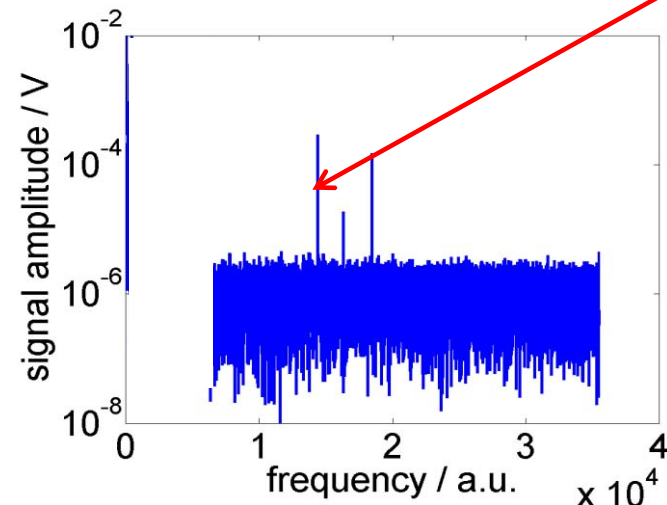
Fourier  
transform

$$D_j = c \frac{f_j}{2 \frac{dv}{dt}}$$

# Traceability to SI: Gas Cell Frequency Reference



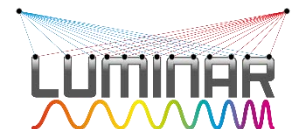
$$D_j = c \frac{n_j}{2\Delta\nu} = \frac{f_j}{2 \frac{d\nu}{dt}}$$



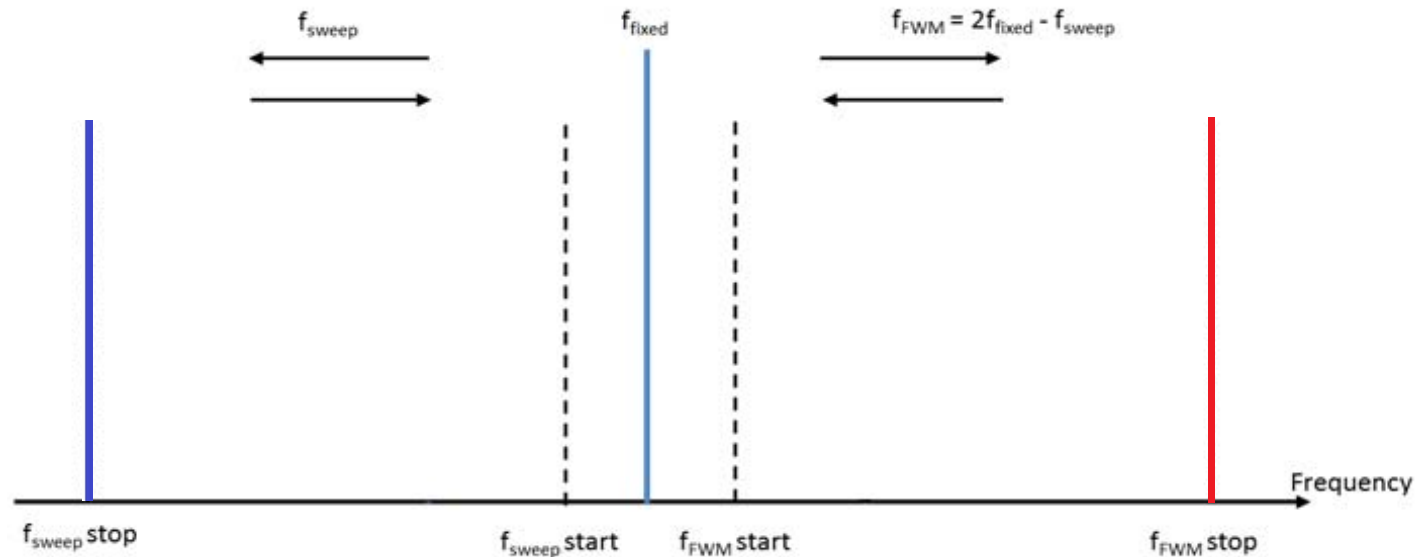
# Vibration compensation

- Conventional solution is to use two lasers; one sweeps up, the other down in frequency
  - Expensive
  - Ideally need to synchronise the sweeps
- We use (degenerate) Four Wave Mixing (FWM)
  - A non-linear optical effect
  - Takes pump laser (fixed frequency,  $F_1$ ), signal laser (tuneable,  $F_2$ ) generates new signals,

$$F_{3,4} = 2F_1 \pm F_2$$



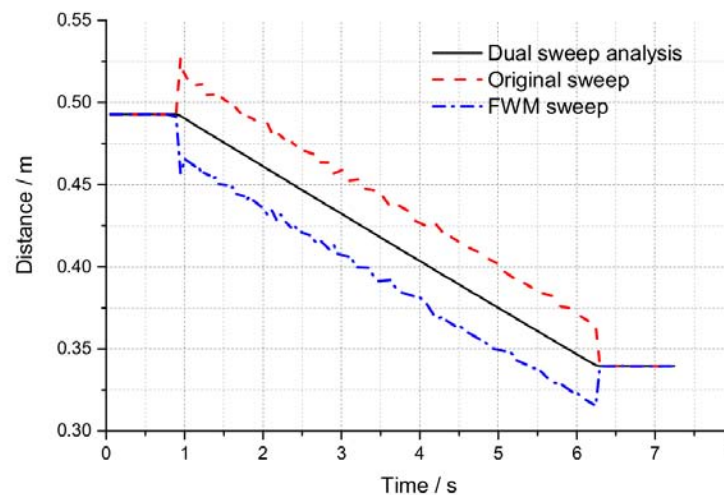
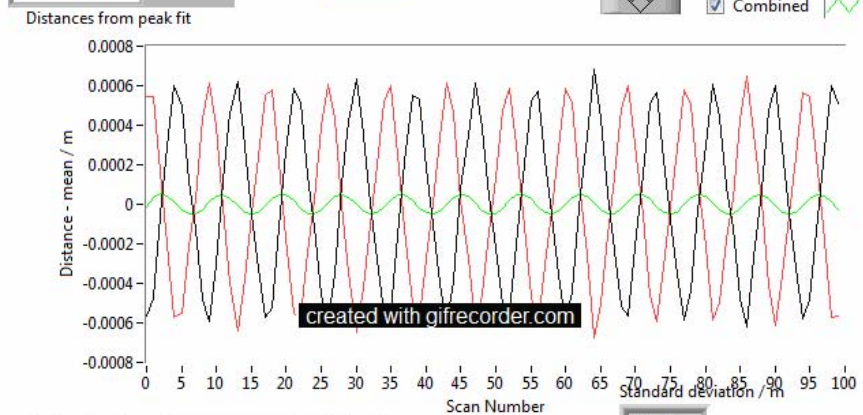
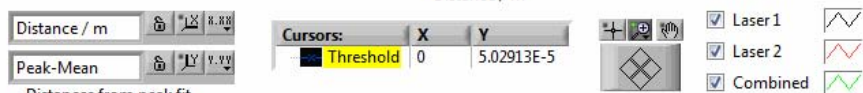
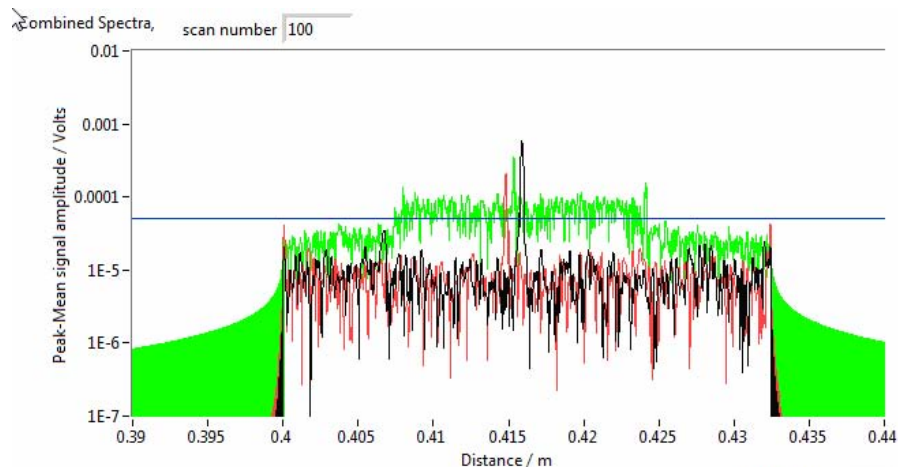
# Vibration Compensation



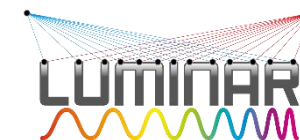
- Fixed frequency DFB laser – 1564.3 nm
- Original laser - 1530 → 1560 nm
- FWM generated - 1565 → 1600 nm
- Filter out unwanted fixed frequency wavelength

# Vibration / Motion Compensation

- Piezoelectric actuator
- 2 Hz frequency
- 0.1 mm amplitude
- Individual sweep amplitudes: 1.3 mm
- Combined sweep amplitude: 0.1 mm



Target moving at 100 mm/s



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# Absolute Distance Measurements

## Divergent beam

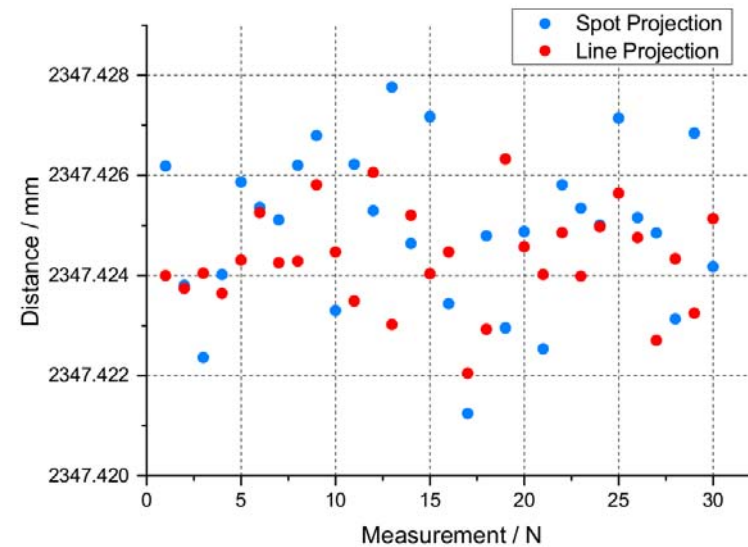
- Maximum distance ~1 m
- Maximum FoV ~ 60

Original laser / $\mu\text{m}$	FWM laser / $\mu\text{m}$	Combined analysis / $\mu\text{m}$
3.8	3.7	0.4

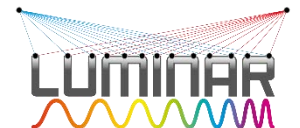
Standard deviation of 100 distance measurements taken of a stationary target at ~ 0.51 m

## Long range system

- Maximum distance > 12 m
- Maximum FoV > 70°
- Greater SNR



30 distance measurements taken of a stationary target at ~ 2.35 m

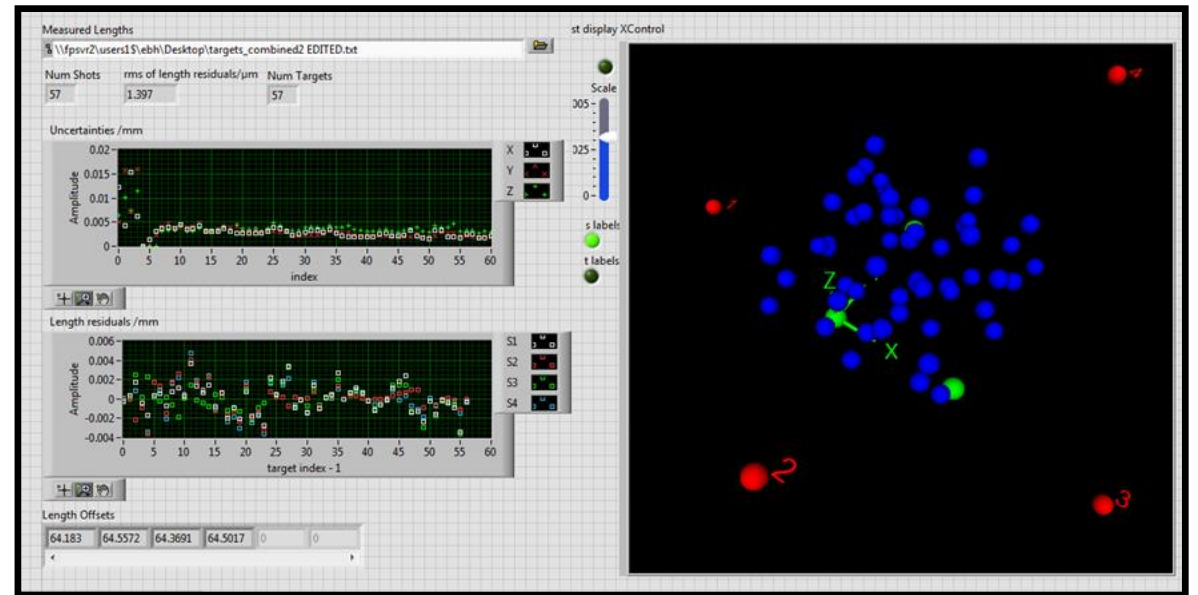


Spot projection/ $\mu\text{m}$	Line projection/ $\mu\text{m}$
1.5	1.0

Standard deviation of 30 distance measurements taken of a stationary target at ~ 2.35 m

# Multilateration Results - Divergent Beam

- Measurement volume of
  - $\sim 0.75 \times 0.75 \times 0.75$  m
- Coordinate uncertainties of  $< 5 \mu\text{m}$  achieved
- RMS length residuals of  $1.4 \mu\text{m}$
- Vibration compensation applied
- But measurements taken sequentially due to SNR issues with FWM



Graphical output of sensor-target positions and associated uncertainties



# Multilateration Results - Long Range Airbus

- 5 x 5 x 3 m measurement volume
- Uncertainties of  $\sim 100 \mu\text{m}$
- Difference from laser tracker for 2.3 m artefact of  $\sim 90 \mu\text{m}$
- Targets measured sequentially
- No vibration compensation



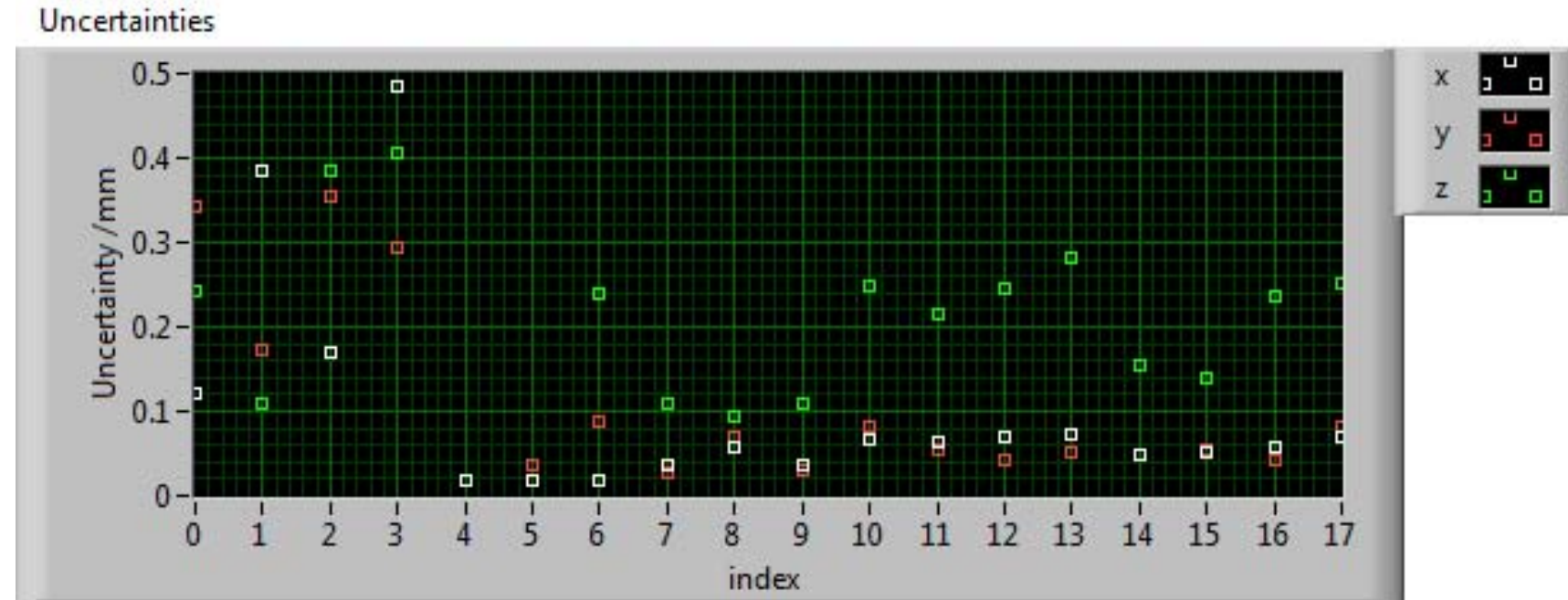
Test setup at Airbus with 4 sensor heads and  
12 targets

# Multilateration Results – Long Range PTB - Decommissioned Nuclear Reactor



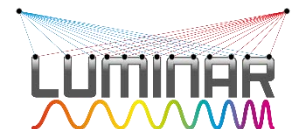
- 10 x 5 x 2.5 m measurement volume
- 4 sensor heads, 15 targets
- Targets measured simultaneously
- Max distance = 8.328 m
- Min distance = 3.240 m
- Angular FoV = 70°

# Multilateration Results – Long Range PTB - Decommissioned Nuclear Reactor



- Measurement uncertainties:
- $x, y \sim 100 \mu\text{m}$ ,  $z \sim 300 \mu\text{m}$
- Difference with tracker measured artefact  $\sim 50 \mu\text{m} - 150 \mu\text{m}$

- No vibration compensation
- Spot projection, not line projection
- No optical distortion correction
- Poor geometry / redundancy



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# Summary and Conclusion

- Prototype *proof-of-concept* system constructed
- Two types of sensor developed
  - Short range (simple diverging lens)L
  - Long range ( SLM + optics + camera)
- Repeatability < 0.5  $\mu\text{m}$  for short range system
- Multi-beam steering over wide angular range using SLM
- FWM for synchronised dual laser sweep generation – vibration/motion compensation
- Simultaneous FSI to multiple targets over large volume from multiple sensors demonstrated
- Traceability through direct, *in-situ* calibration against a gas absorption cell with an uncertainty of 1 ppm.
- Multilateration determines un-known system parameter, currently sensor locations and offsets as well as target coordinates
- Currently achieving uncertainties ~ 100  $\mu\text{m}$  (but lots of improvements coming)
- Three patents pending

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# Future Work

## Lots to do!

- Improve mechanical stability of sensors
- Fix FWM – vibration/motion compensation
- Improve optics for long-range sensor
- Software improvements/integration
- Implement optics calibration in multilateration solution – improve accuracy
- Develop (much) faster data acquisition system – increase measurement speed, implement target tracking
- .....

# Thank you

National  
Measurement  
System



## EMRP

European Metrology Research Programme  
► Programme of EURAMET



The EMRP is jointly funded by the EMRP participating countries within EURAMET and the European Union

